

REVIEW SECTIONS:

$$[15] \rightarrow 71, 77$$

$$\begin{array}{rcl} 71. & -5 \leq 4 - 3x \leq 2 \\ & -4 & -4 \\ & -9 \leq -3x \leq -2 \\ & \frac{-9}{-3} \leq \frac{-3x}{-3} \leq \frac{-2}{-3} \end{array}$$

$$3 \geq x \geq \frac{2}{3}$$

$$\boxed{\frac{2}{3} \leq x \leq 3}$$

$$\boxed{[\frac{2}{3}, 3]}$$

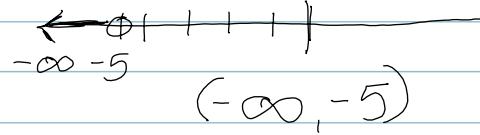
$$\begin{array}{l} 77. (x+2)(x-3) > (x-1)(x+1) \\ x^2 - 3x + 2x - 6 > x^2 - x + x - 1 \\ x^2 - x - 6 > x^2 - 1 \\ -x^2 & -x^2 \\ -x - 6 > -1 \\ +6 & +6 \\ -x > 5 \\ \boxed{x < -5} \end{array}$$

$$-x - 6 > -1$$

$$+6 & +6$$

$$-x > 5$$

$$\boxed{x < -5}$$



Ex: ~~$1 < x + 4$~~
 ignore \uparrow $1 < x + 4$

$$75. 1 < 1 - \frac{1}{2}x < 4 \quad * \text{Find LCD}$$

LCD = 2

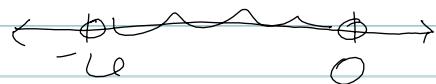
$$2 < 2 - 1x < 8$$

$$-2 \quad -2 \quad -2$$

$$\frac{0}{-1} < -\frac{x}{-1} < \frac{6}{-1}$$

$$\frac{0}{-6} > x > \frac{6}{-1}$$

always from least to greatest



$$11.6 \rightarrow 41, 53$$

$$(41) |3t-2| \leq 4$$

less than \rightarrow and (common)

$$3t-2 \leq 4 \quad \text{and} \quad 3t-2 \geq -4$$

$$+2 \quad +2$$

$$3t \leq 6$$

$$t \leq 2$$



$$\begin{array}{ccccccc} & & & & & & \\ & - & & & + & & \\ \hline & | & | & | & | & | & | \\ & -1 & & 0 & & 1 & 2 \\ & & & \nearrow & & & \\ & & & -\frac{2}{3} & & & \end{array}$$

$$\left[-\frac{2}{3}, 2\right]$$

[SHORT CUT]:

$$3t-2 \leq 4 \text{ AND } 3t-2 \geq -4$$

$$-4 \leq 3t-2$$

$$-4 \leq 3t-2 \leq 4$$

solve from here

$$|x| < a \rightarrow -a < x < a$$

$$(53) -|2x-1| \geq -3$$

$$|2x-1| \leq 3$$

and
(common)

$$2x-1 \leq 3 \quad \text{and} \quad 2x-1 \geq -3$$

$$+1 \quad +1$$

$$2x \leq 4$$

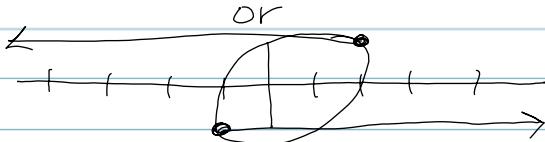
$$x \leq 2 \text{ and}$$

$$+1 \quad +1$$

$$2x \geq -2$$

$$x \geq -1$$

$$-1 \leq x \leq 2$$



$$[-1, 2]$$

$$\textcircled{25} \quad \cancel{5} \mid \frac{1}{2} \cancel{x}$$

$$|x^2 - 9| = 0$$

$$x^2 - 9 = 0$$

$$(x+3)(x-3) = 0$$

$$x+3=0 \quad x=-3$$

$$x-3=0 \quad x=3$$

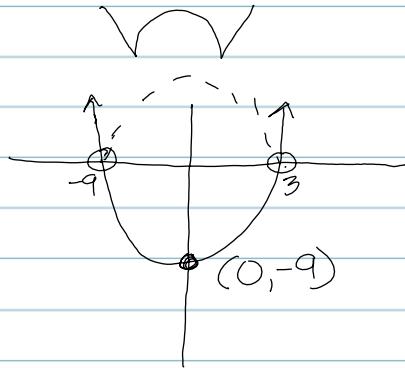
$$x^2 - 9 = 0$$

$$x^2 = 9$$

$$\sqrt{x^2} = \sqrt{9}$$

$$x = \pm \sqrt{9}$$

$$x = \pm 3$$



$$\textcircled{31} \quad \left| \frac{3x-2}{2x-3} \right| = 2$$

$$\frac{3x-2}{2x-3} = 2$$

$$\frac{3x-2}{2x-3} = -2$$

$$3x-2 = 2(2x-3)$$

$$3x-2 = 4x-6$$

$$-3x$$

$$-2 = x-6$$

$$+6 \qquad +6$$

$$4 = x$$

$$\left\{ \frac{8}{7}, 4 \right\}$$

$$3x-2 = -2(2x-3)$$

$$3x-2 = -4x+6$$

$$+4x \qquad +4x$$

$$7x-2 = 6$$

$$+2 \qquad +2$$

$$7x = 8$$

$$x = \frac{8}{7}$$

REVIEW → 27, 17, 21, 69

$$\textcircled{17} \quad \sqrt[3]{x^2 - 1} = 2$$

$$\left(\sqrt[3]{x^2 - 1} \right)^3 = 2^3$$

$$x^2 - 1 = 8$$

$$x^2 = 9 \quad \text{or} \quad x^2 - 9 = 0$$

$$x = \pm 3$$

$$\textcircled{21} \quad x^4 - 5x^2 + 4 = 0$$

$$(x^2 - 4)(x^2 - 1) = 0$$

$$(x+2)(x-2)(x-1)(x+1) = 0$$

$$x+2=0 \rightarrow x = -2$$

$$x-2=0$$

$$x-1=0$$

$$x+1=0$$

$$x = -1$$

$$\{-2, -1, 1, 2\}$$

$$(27) \quad \sqrt{x+1} + \sqrt{x-1} = \sqrt{2x+1}$$

$$(\sqrt{x+1} + \sqrt{x-1})^2 = (\sqrt{2x+1})^2$$

$$(\sqrt{x+1} + \sqrt{x-1})(\sqrt{x+1} + \sqrt{x-1}) = 2x+1$$

$$\frac{(x+1) + \sqrt{(x+1)(x-1)}}{x} + \frac{\sqrt{(x-1)(x+1)}}{\sqrt{(x-1)(x+1)}}$$

$$+ \frac{(x+1)}{-x} - \frac{2x}{2x} = 2x+1$$

$$2\sqrt{(x+1)(x-1)} = 1$$

$$4(x+1)(x-1) = 1$$

$$4(x^2 - 1) = 1$$

$$4x^2 - 4 = 1$$

$$4x^2 = 5$$

$$x^2 = \frac{5}{4}$$

$$x = \pm \sqrt{\frac{5}{4}} = \pm \frac{\sqrt{5}}{2}$$

potential answers

CHECK:

~~$x = -\frac{\sqrt{5}}{2}$~~

$$x = \frac{\sqrt{5}}{2}$$

$$\sqrt{x+1} + \sqrt{x-1} = \sqrt{2x+1}$$

$$\sqrt{x+1} + \sqrt{x-1} = \sqrt{2x+1}$$

OR USE CALCULATOR

$$\sqrt{\frac{-\sqrt{5}}{2} + 1} + \sqrt{\frac{-\sqrt{5}}{2} - 1} = \sqrt{2(-\sqrt{5}) + 1}$$

$$\sqrt{\frac{\sqrt{5}}{2} + 1} + \sqrt{\frac{\sqrt{5}}{2} - 1} = \sqrt{2(\frac{\sqrt{5}}{2}) + 1}$$

- neg.

$$x = \frac{\sqrt{5}}{2} \approx 1.12$$

$$\sqrt{1.12 + 1} + \sqrt{1.12 - 1} = \sqrt{2(1.12) + 1}$$

$$\sqrt{2.12} + \sqrt{0.12} = \sqrt{3.24}$$

$$1.456 + 0.346 = 1.8$$

$$1.802 \approx 1.8 \checkmark$$

(A) $(2+3i)^3$; form $a+bi$

$$\begin{aligned} & (2+3i)(2+3i)(2+3i) & i = \sqrt{-1} \\ & (2+3i)(4+6i+6i+9i^2) & i^2 = -1 \\ & & 9(-1) \end{aligned}$$

$$\begin{aligned} & (2+3i)(-5+12i) & -9 \\ & -10 + 24i - 15i + 36i^2 & \\ & & 36(-1) \\ & & \rightarrow -36 \end{aligned}$$

$$-16 + 9i$$